

反射テスト 展開公式 入試問題 計算の工夫 03

1. 次の式を計算せよ。(S級1分50秒, A級2分30秒, B級4分, C級6分)

$$(1) \quad (4.5^2 - 1.5^2) \times \left(-\frac{1}{2}\right)^2 - \left(0.6 - \frac{1}{3}\right) \div \frac{2}{5}$$

$$(2) \quad 39 \times 213 - 40 \times 210 - 41 \times 209 + 42 \times 207$$

2. 次の式を計算せよ。(S級1分50秒, A級2分30秒, B級4分, C級6分)

(1) $(3.25^2 - 1.25^2) \times \left(-\frac{2}{3}\right)^3 - \left(0.2 - \frac{4}{3}\right) \div \frac{3}{5}$

(2) $190 \times 1950 - 188 \times 1949 - 189 \times 1948 + 187 \times 1947$

反射テスト 展開公式 入試問題 計算の工夫 03 解答解説

1. 次の式を計算せよ。(S級1分50秒, A級2分30秒, B級4分, C級6分)

$$(1) \quad (4.5^2 - 1.5^2) \times \left(-\frac{1}{2}\right)^2 - \left(0.6 - \frac{1}{3}\right) \div \frac{2}{5}$$

$$\begin{aligned} \text{与式} &= (4.5 + 1.5)(4.5 - 1.5) \times \frac{1}{4} - \left(\frac{3}{5} - \frac{1}{3}\right) \times \frac{5}{2} \\ &= 6 \times 3 \times \frac{1}{4} - \frac{9-5}{15} \times \frac{5}{2} \\ &= \frac{9}{2} - \frac{4}{15} \times \frac{5}{2} \\ &= \frac{9}{2} - \frac{2}{3} \\ &= \frac{27-4}{6} \\ &= \frac{23}{6} \end{aligned}$$

$$(2) \quad 39 \times 213 - 40 \times 210 - 41 \times 209 + 42 \times 207$$

$a = 40$, $b = 210$ とおくと,

$$\begin{aligned} \text{与式} &= (a-1)(b+3) - ab - (a+1)(b-1) + (a+2)(b-3) \\ &= ab + 3a - b - 3 - ab - (ab - a + b - 1) + ab - 3a + 2b - 6 \\ &= ab + 3a - b - 3 - ab - ab + a - b + 1 + ab - 3a + 2b - 6 \\ &= a - 8 \\ &= \mathbf{32} \end{aligned}$$

2. 次の式を計算せよ。(S級1分50秒, A級2分30秒, B級4分, C級6分)

$$(1) \quad (3.25^2 - 1.25^2) \times \left(-\frac{2}{3}\right)^3 - \left(0.2 - \frac{4}{3}\right) \div \frac{3}{5}$$

$$\begin{aligned} \text{与式} &= (3.25 + 1.25)(3.25 - 1.25) \times \left(-\frac{8}{27}\right) - \left(\frac{1}{5} - \frac{4}{3}\right) \times \frac{5}{3} \\ &= -4.5 \times 2 \times \frac{8}{27} - \frac{3-20}{15} \times \frac{5}{3} \\ &= -\frac{9}{2} \times 2 \times \frac{8}{27} + \frac{17}{15} \times \frac{5}{3} \\ &= -\frac{8}{3} + \frac{17}{9} \\ &= -\frac{24}{9} + \frac{17}{9} \\ &= -\frac{7}{9} \end{aligned}$$

$$(2) \quad 190 \times 1950 - 188 \times 1949 - 189 \times 1948 + 187 \times 1947$$

$a = 190$, $b = 1950$ とおくと,

$$\begin{aligned} \text{与式} &= ab - (a-2)(b-1) - (a-1)(b-2) + (a-3)(b-3) \\ &= ab - (ab - a - 2b + 2) - (ab - 2a - b + 2) + ab - 3a - 3b + 9 \\ &= ab - ab + a + 2b - 2 - ab + 2a + b - 2 + ab - 3a - 3b + 9 \\ &= 5 \end{aligned}$$